More Series Practice Problems

Determine whether each of the following series is convergent or divergent.

1.
$$\sum_{n=1}^{\infty} \frac{n}{n^3 + 1}$$

$$2. \sum_{n=1}^{\infty} \frac{n^3}{5^n}$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n\sqrt{\ln n}}$$

$$4. \sum_{n=1}^{\infty} \ln \left(\frac{n}{3n+1} \right)$$

5.
$$\sum_{n=1}^{\infty} \frac{(-5)^{2n}}{n^2 9^n}$$

6.
$$\sum_{n=1}^{\infty} \frac{\cos^2 n}{n^2 + 1}$$

7.
$$\sum_{n=1}^{\infty} \frac{4+3^n}{2^n}$$

8.
$$\sum_{n=0}^{\infty} \frac{(-10)^n}{n!}$$

9.
$$\sum_{n=1}^{\infty} \frac{10^n}{(n+1)4^{2n+1}}$$

10.
$$\sum_{n=1}^{\infty} \frac{n^2}{5^n}$$

11.
$$\sum_{n=1}^{\infty} (-1)^{n-1} \frac{2^n}{n^4}$$

12.
$$\sum_{n=1}^{\infty} \frac{n^2 - 1}{3n^4 + 1}$$

Determine whether each of the following series is convergent or divergent. If the series is convergent, find its sum.

1.
$$\sum_{n=1}^{\infty} \frac{2^{2n+1}}{5^n}$$

2.
$$\sum_{n=1}^{\infty} \left(\frac{3}{n(n+1)} + \frac{1}{2^n} \right)$$

3.
$$\sum_{n=0}^{\infty} \frac{\pi^n}{3^{n+1}}$$

4.
$$\sum_{n=1}^{\infty} \frac{(-6)^{n-1}}{5^{n-1}}$$

$$5. \sum_{n=0}^{\infty} 5\left(\frac{2}{3}\right)^n$$

$$6. \sum_{n=1}^{\infty} (\cos 1)^n$$

7.
$$\sum_{n=1}^{\infty} \frac{3}{n(n+3)}$$

$$8. \sum_{n=1}^{\infty} \ln \left(\frac{n}{n+1} \right)$$