

Section 3.4, page 164

7. $y = c_1 e^t \cos t + c_2 e^t \sin t$
 9. $y = c_1 e^{-2t} + c_2 e^{-4t}$
 11. $y = c_1 e^{-3t} \cos 2t + c_2 e^{-3t} \sin 2t$
 13. $y = c_1 e^{-t} \cos(t/2) + c_2 e^{-t} \sin(t/2)$
 15. $y = c_1 e^{-t/2} \cos t + c_2 e^{-t/2} \sin t$
 17. $y = \frac{1}{2} \sin 2t$; steady oscillation
 18. $y = e^{-2t} \cos t + 2e^{-2t} \sin t$; decaying oscillation
 19. $y = -e^{t-\pi/2} \sin 2t$; growing oscillation
 20. $y = (1+2\sqrt{3}) \cos t - (2-\sqrt{3}) \sin t$; steady oscillation
 21. $y = 3e^{-t/2} \cos t + \frac{5}{2}e^{-t/2} \sin t$; decaying oscillation
 22. $\dot{y} = \sqrt{2} e^{-(t-\pi/4)} \cos t + \sqrt{2} e^{-(t-\pi/4)} \sin t$; decaying oscillation
 23. (a) $u = 2e^{t/6} \cos(\sqrt{23}t/6) - (2/\sqrt{23})e^{t/6} \sin(\sqrt{23}t/6)$
 (b) $t = 10.7598$
 24. (a) $u = 2e^{-t/5} \cos(\sqrt{34}t/5) + (7/\sqrt{34})e^{-t/5} \sin(\sqrt{34}t/5)$
 (b) $T = 14.5115$
 25. (a) $y = 2e^{-t} \cos \sqrt{5}t + [(\alpha+2)/\sqrt{5}]e^{-t} \sin \sqrt{5}t$
 (b) $\alpha = 1.50878$
 (c) $t = [\pi - \arctan(2\sqrt{5}/(2+\alpha))]/\sqrt{5}$
 (d) $\pi/\sqrt{5}$
 26. (a) $y = e^{-at} \cos t + ae^{-at} \sin t$
 (b) $T = 1.8763$
 (c) $\alpha = \frac{1}{4}$, $T = 7.4284$; $\alpha = \frac{1}{2}$, $T = 4.3003$; $\alpha = 2$, $T = 1.5116$
 35. Yes, $y = c_1 \cos x + c_2 \sin x$, $x = \int e^{-t^2/2} dt$
 36. No
 37. Yes, $y = c_1 e^{-t^2/4} \cos(\sqrt{3}t^2/4) + c_2 e^{-t^2/4} \sin(\sqrt{3}t^2/4)$
 39. $y = c_1 \cos(\ln t) + c_2 \sin(\ln t)$
 41. $y = c_1 t^{-1} \cos(\frac{1}{2} \ln t) + c_2 t^{-1} \sin(\frac{1}{2} \ln t)$
 40. $y = c_1 t^{-1} + c_2 t^{-2}$
 42. $y = c_1 t^6 + c_2 t^{-1}$

Section 3.5, page 172

1. $y = c_1 e^t + c_2 t e^t$
 3. $y = c_1 e^{-t/2} + c_2 e^{3t/2}$
 5. $y = c_1 e^t \cos 3t + c_2 e^t \sin 3t$
 7. $y = c_1 e^{-t/4} + c_2 e^{-4t}$
 9. $y = c_1 e^{2t/5} + c_2 t e^{2t/5}$
 11. $y = 2e^{2t/3} - \frac{1}{3}te^{2t/3}$, $y \rightarrow -\infty$ as $t \rightarrow \infty$
 12. $y = 2te^{3t}$, $y \rightarrow \infty$ as $t \rightarrow \infty$
 13. $y = -e^{-t/3} \cos 3t + \frac{5}{3}e^{-t/3} \sin 3t$, $y \rightarrow 0$ as $t \rightarrow \infty$
 14. $y = 7e^{-2(t+1)} + 5te^{-2(t+1)}$, $y \rightarrow 0$ as $t \rightarrow \infty$
 15. (a) $y = e^{-3t/2} - \frac{5}{2}te^{-3t/2}$
 (b) $t = \frac{2}{3}$
 (c) $t_0 = 16/15$, $y_0 = -\frac{5}{3}e^{-8/5} \cong -0.33649$
 (d) $y = e^{-3t/2} + (b + \frac{3}{2})te^{-3t/2}$; $b = -\frac{3}{2}$
 16. $y = 2e^{t/2} + (b-1)te^{t/2}$; $b = 1$
 17. (a) $y = e^{-t/2} + \frac{5}{2}te^{-t/2}$
 (b) $t_M = \frac{8}{5}$, $y_M = 5e^{-4/5} \cong 2.24664$
 (c) $y = e^{-t/2} + (b + \frac{1}{2})te^{-t/2}$
 (d) $t_M = 4b/(1+2b) \rightarrow 2$ as $b \rightarrow \infty$;
 $y_M = (1+2b) \exp[-2b/(1+2b)] \rightarrow \infty$ as $b \rightarrow \infty$
 18. (a) $y = ae^{-2t/3} + (\frac{2}{3}a-1)te^{-2t/3}$
 (b) $a = \frac{3}{2}$
 23. $y_2(t) = t^3$
 25. $y_2(t) = t^{-1} \ln t$
 27. $y_2(x) = \cos x^2$
 24. $y_2(t) = t^{-2}$
 26. $y_2(t) = te^t$
 28. $y_2(x) = x$