

Math 333
Quiz 1
Tuesday, January 22, 2008

1. Consider the population model

$$\frac{dP}{dt} = 0.4P \left(1 - \frac{P}{100}\right) \left(\frac{P}{25} - 1\right),$$

where $P(t)$ is the population at time t .

- (a) For what values of P is the population in equilibrium?

- (b) For what values of P is the population increasing?

- (c) For what values of P is the population decreasing?

2. Find all solutions of the differential equation

$$\frac{dy}{dt} = 2(y^2 - 4)te^{t^2}.$$

3. Solve the initial-value problem

$$\frac{dy}{dx} = \frac{x - y}{x + y}, \quad y(1) = 1.$$