- 1) Let a and b be positive constants. Show that if f is  $O(\log_a n)$  then f is also  $O(\log_b n)$ .
- 2) Suppose the size of the input is doubled for an algorithm (going from n to 2n). Explain how the number of operations change for the algorithm if its Big-O complexity is
- a) O(n)
- b)  $O(n^2)$
- c)  $O(\log(n))$
- d)  $O(2^n)$

What if the size of the input increases by 1 (going from n to n + 1)?

3) Rank the following functions according to how fast they grow as  $n \to \infty$ :  $n \log^2(n), \log^{2019}(n), \sqrt{n}, n^2, n!, \sqrt{2}^n, n^n$ .

Determine the running time of the following program segments in Big-O notation. Take the size of the input as n, unless otherwise stated.

```
4)
    double sum=0;
    for(int i=0; i<1000000;i++)
        sum+=sqrt(i);
5)
    while(n>1)
    {
        n=n/2;
        cout<<"This is a useless code";</pre>
    }
6)
int count=0;
for(i=0;i<n;i++)
{
    count++;
}
```

What happens if we take the size of the input as log(n) as opposed to n?

```
8)
for(i=0;i<n;i++)
{
    for(j=0;j<n;j++)</pre>
    {
         count++;
    }
}
a) Considering the size of the input as n
b) Considering the size of the input as log(n)
9)
for(i=0;i<n;i++)</pre>
    for(j=i;j< n;j++)
         count++;
    }
}
10)
int i, j,k;
for(k=0;k<n;k++)
}
 for(i=0;i<n;i++)
 {
    j=n;
    while(j>1)
         j=j/3;
         cout<<i*j*k<<endl;</pre>
    }
 }
}
for(i=0;i<n;i++)
{
    cout<<i*i<<endl;</pre>
}
```