Problem 3: How to Tile?

A 23×23 square is to be completely tiled by $1 \times 1, 2 \times 2$, and 3×3 tiles. What is the minimum number of 1×1 tiles needed?

As always, show your work, fully explain and justify your answer. A solution mainly obtained by computers or calculators will not be accepted.