Problem of the Week-4: A Logarithmic Sum

Find the value of the sum

$$\lfloor \log_8 1 \rfloor + \lfloor \log_8 2 \rfloor + \dots + \lfloor \log_8 1000 \rfloor$$

where $\lfloor x \rfloor$ denotes the floor of x, the largest integer less than or equal to x

As always, show your work, fully explain and justify your answer. No calculators or computers.

Posting Date 2/19/14. Submit solutions to Noah Aydin, Mathematics Department, RBH 319 (e-mail or hard-copy, but hard copy submissions must include a time stamp) by 4 pm on 2/28/14.