Problem of the Week-5: Largest Factor

Determine the largest integer that is a divisor of

$$n^5 - 17n^3 + 16n$$

for all $n \geq 4$.

As always, explain and justify your answer.