

## The Blob

(OZ, Vol 1. page 264)

A certain menacing biological culture (aka “The Blob”) grows at a rate proportional to its size. When it arrived unnoticed one Wednesday noon in Chicago’s loop, it weighed just one gram. By the 4 p.m. rush hour it weighed 4 grams.

The Blob has its “eye” on the Sears Tower, a tasty morsel weighing around  $3 \times 10^{12}$  grams. As soon as The Blob weighs 1000 times as much (i.e.  $3 \times 10^{15}$  grams), it intends to *eat* the Sears Tower. By what time must the Blob be stopped? Will Friday’s rush hour be delayed?

## Newton’s Law of Cooling

(OZ, Vol 1. page 255)

It’s a winter day in Frostbite Falls, Minnesota---10 degrees below zero Celsius. Boris and Natasha stop at a convenience store for hot (initially  $90^\circ\text{C}$ ) coffee to warm them on the cold, windy walk home. Two types of cups are available, environmentally destructive foam and politically correct cardboard.

Boris wants foam. “What do I care about the greenhouse effect?” he asks. “Besides, remember the proportionality constant  $k$  in Newton’s law of cooling

$$y' = k(y - C)$$

where  $C$  is the ambient temperature,  $y$  is the Celsius temperature of the coffee at time  $t$ , and  $t$  is the time measured in minutes? Well, for foam,  $k = -.05$ . For cardboard,  $k$  is a pathetic  $-.08$ .”

“Do what you want, Boris,” says Natasha. “I’d rather save the world. I’m having cardboard. And make mine decaf.”

- How long does Boris’s coffee stay above 70 degrees? How about Natasha’s? How hot is each cup after 5 minutes?
- Redo part (a) assuming that Boris and Natasha drink their coffee in the overheated ( $25^\circ\text{C}$ ) convenience store.
- What value of  $k$  is needed to assure that the coffee, starting at  $90^\circ\text{C}$ , is still  $70^\circ\text{C}$  after 5 minutes outdoors. [Hint: use the solution function to set up an appropriate equation, then solve for  $k$ .]

## Carbon Dating.

(From *Calculus in Context*, pg. 228)

Virtually all living things take up carbon as they grow. This carbon comes in two principal forms: Normal stable carbon  $^{12}\text{C}$ —and radioactive carbon--  $^{14}\text{C}$ .  $^{14}\text{C}$  decays at a rate proportional to the amount of  $^{14}\text{C}$  remaining. While the organism is alive, this lost  $^{14}\text{C}$  is continually replenished. After the organism dies, though,  $^{14}\text{C}$  is no longer replaced, so the percentage of  $^{14}\text{C}$  decreases exponentially over time. It is found that after 5730 years, half of the original  $^{14}\text{C}$  remains. If an archeologist finds a bone with only 20% of the original  $^{14}\text{C}$  present, how old is the bone?