

Homework: DCT for Improper Integrals

Calculus II, Math 112

Name: _____

1. For each of the following integrals, use the Direct Comparison Test to determine if the integral converges or diverges. Show all work.

(a) $\int_1^{\infty} \frac{\cos^2(x)}{1+x^2} dx$

(b) $\int_1^{\infty} \frac{1}{\sqrt{x^3+1}} dx$

(c) $\int_1^{\infty} \frac{dx}{x+e^x}$

(d) $\int_1^{\infty} \frac{dx}{x+e^{2x}}$

(e) $\int_3^{\infty} \frac{dx}{x-e^{-x}}$

(f) $\int_1^{\infty} \frac{\sqrt{1+\sqrt{x}}}{\sqrt{x}} dx$

(g) $\int_1^{\infty} \frac{dx}{x+e^{2x}}$

(h) $\int_1^{\infty} \frac{1+3\sin^4(2x)}{\sqrt{x}} dx$

(i) $\int_1^{\infty} \frac{e^{-x}}{x} dx$

(j) $\int_1^{\infty} \frac{e^{-x^2}}{x} dx$

(k) $\int_0^{\infty} \frac{e^{-x^2}}{x} dx$

(l) $\int_0^{\frac{\pi}{2}} \frac{dx}{x \sin(x)}$