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**Math 224**  
**Quiz 6**  
**Thursday, November 15, 2007**

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**Note:** You are allowed to use Maple for computation of dot products, addition of vectors, row reduction, etc. on this quiz, but you must **SHOW ALL WORK** to receive credit. In particular, you may not use the GramSchmidt command in Maple to produce an orthogonal or orthonormal basis (you may, however, use it to check your work). If you need more space for your work, use the back of the pages and/or attach additional sheets.

1. Find the projection of  $[-1, 2, 0, 1]$  on  $sp([2, -3, 1, 2])$  in  $\mathbb{R}^4$ .

2. Find the orthogonal complement of  $W = sp([1, 3, 0], [2, 1, 4])$ .

3. Find an orthonormal basis for the subspace  $sp([0, 1, 0], [1, 1, 1])$  of  $\mathbb{R}^3$ .

4. Let  $W$  be a subspace of  $\mathbb{R}^n$  with orthogonal complement  $W^\perp$ . Let  $\mathbf{b}$  be any vector in  $\mathbb{R}^n$ . Writing  $\mathbf{b} = \mathbf{b}_W + \mathbf{b}_{W^\perp}$ , where  $\mathbf{b}_W$  is in  $W$  and  $\mathbf{b}_{W^\perp}$  is in  $W^\perp$ , prove that

$$\|\mathbf{b}\| = \sqrt{\|\mathbf{b}_W\|^2 + \|\mathbf{b}_{W^\perp}\|^2}.$$

Hint: Use  $\|\mathbf{b}\|^2 = \mathbf{b} \cdot \mathbf{b}$ .